

# Faites des paquets de preuves avec Why3 !

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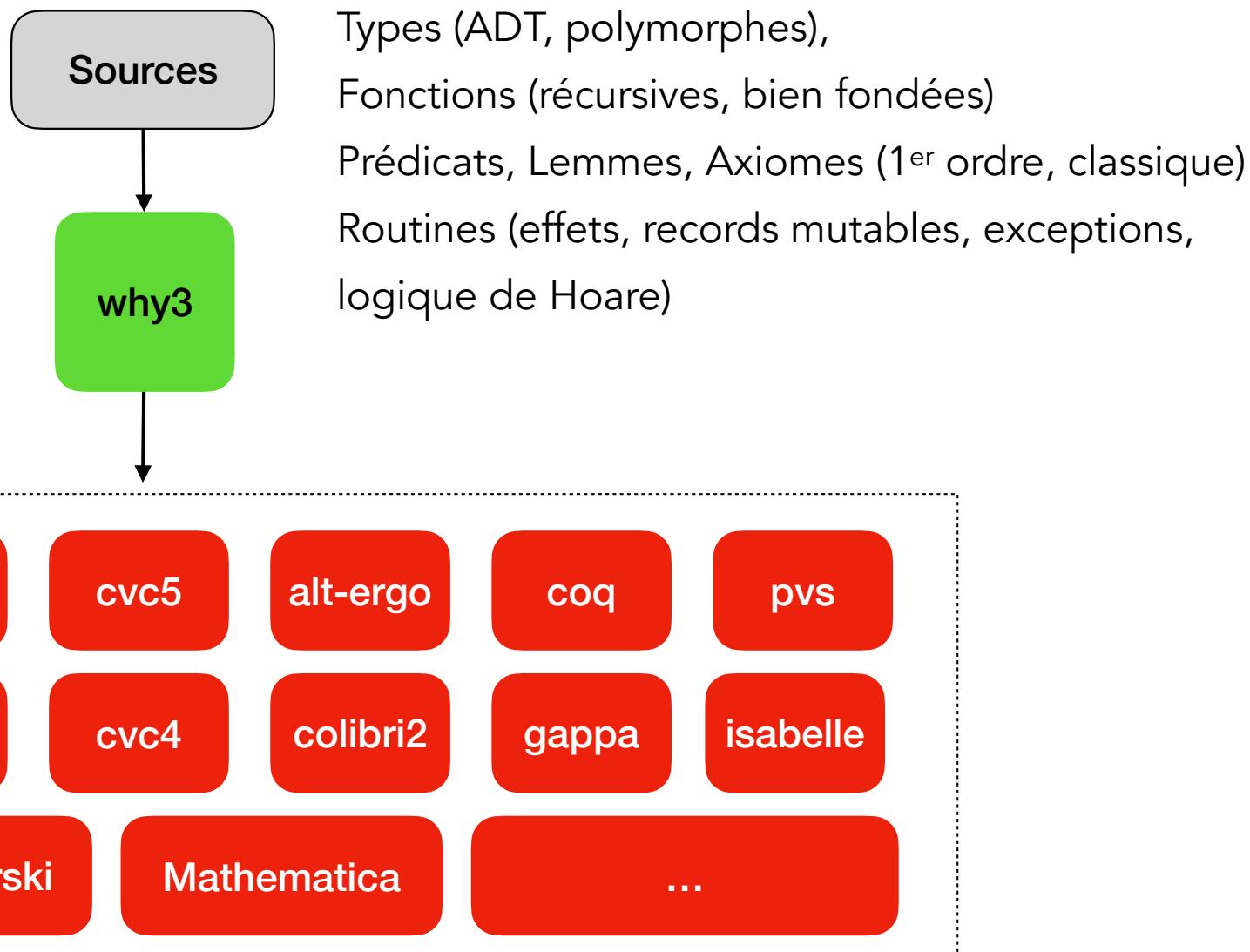
Loïc Correnson  
CEA-LIST, Laboratoire de Sûreté Logicielle

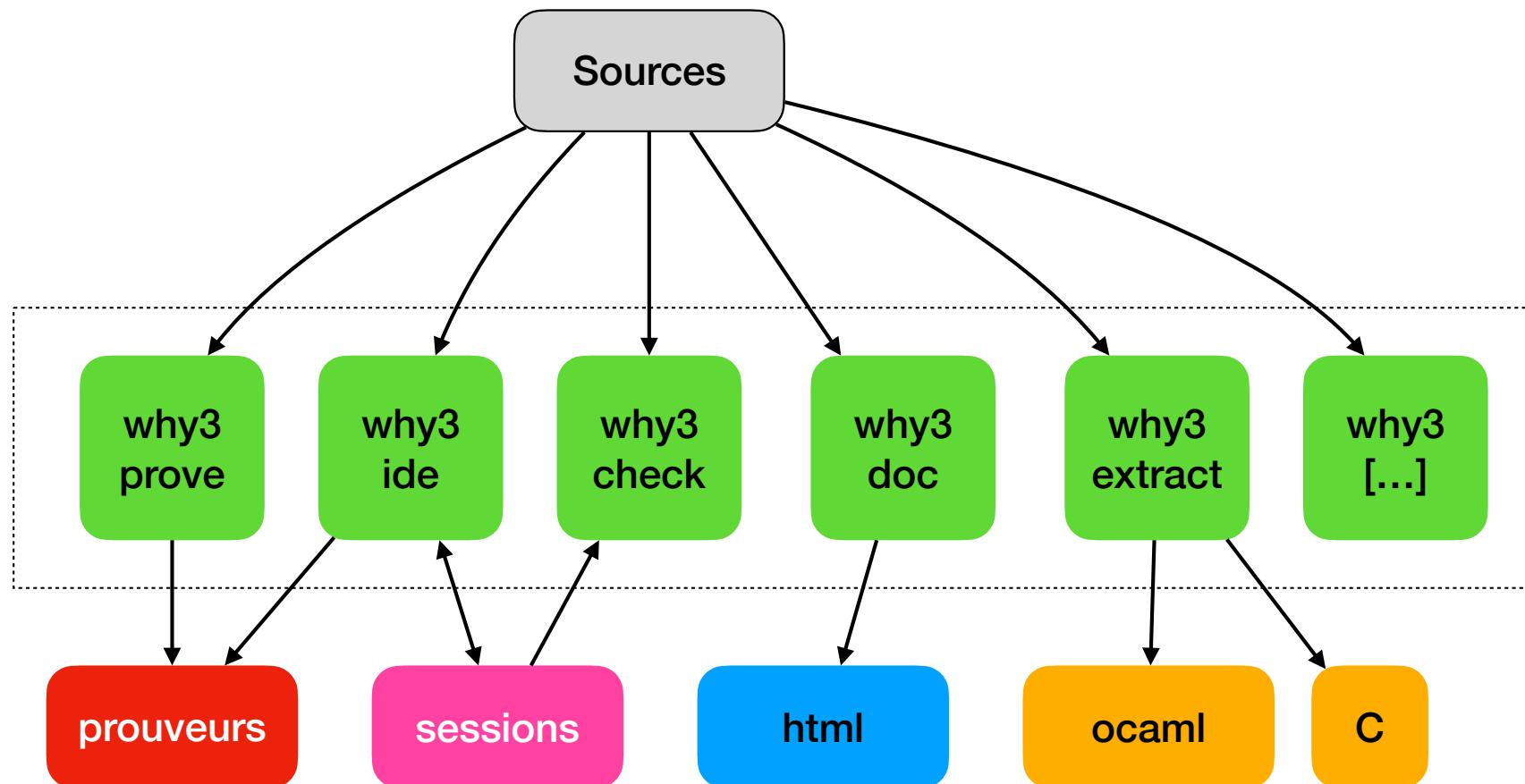
JFLA 2024

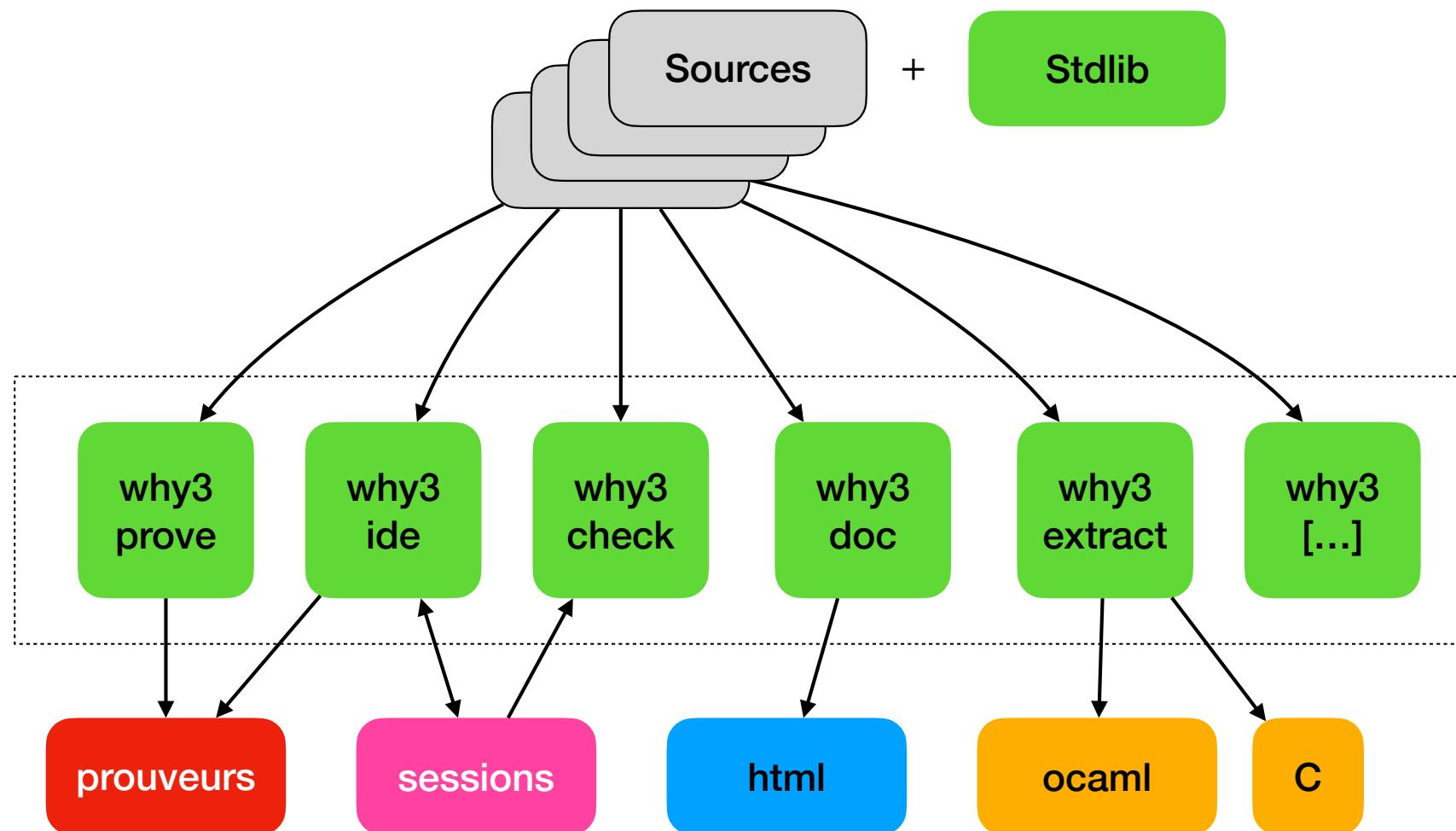
# Why3

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Faut-il le présenter ?

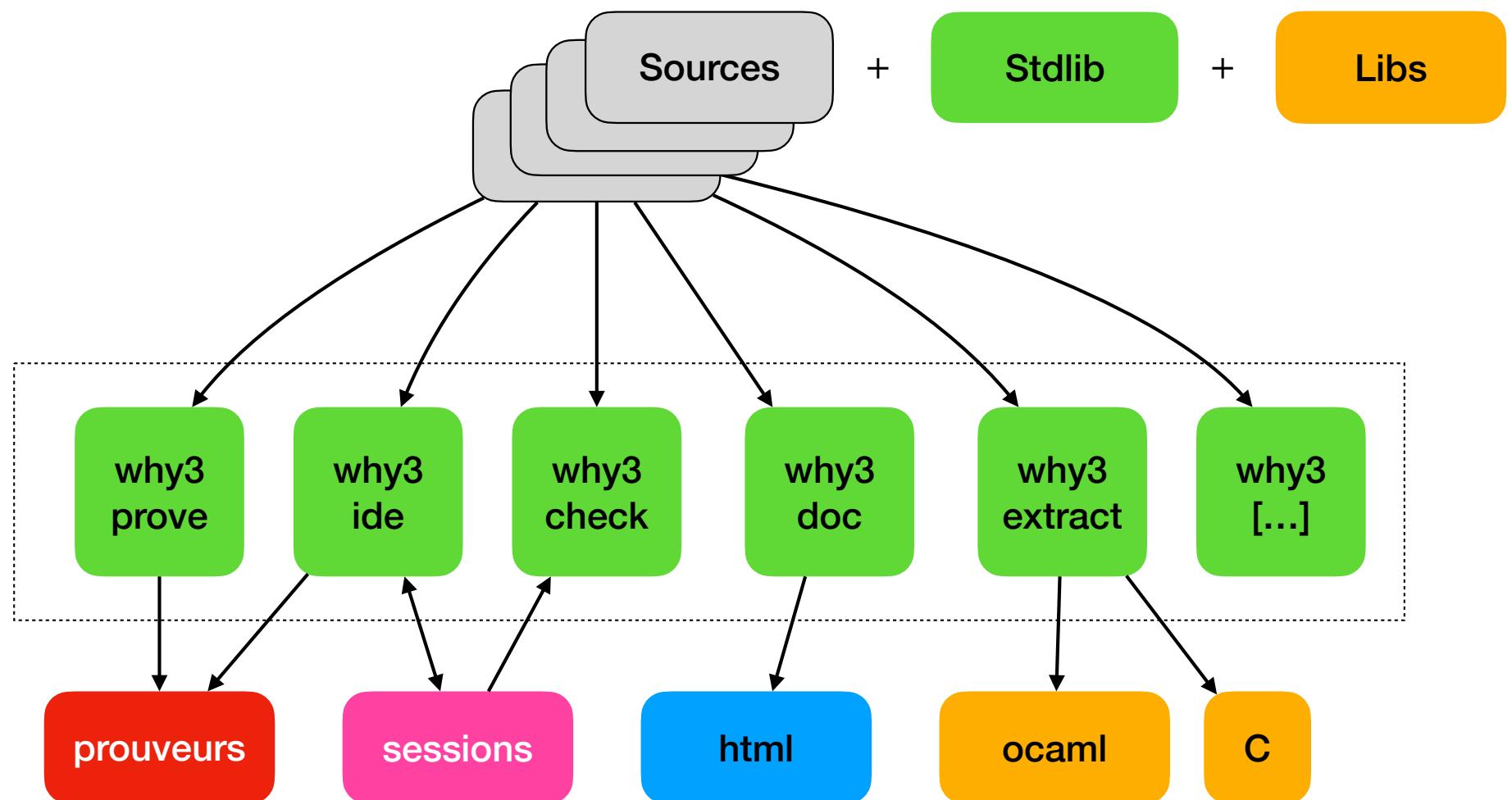






# Why3

## Where Programs Meet Provers



# Plein de preuves !

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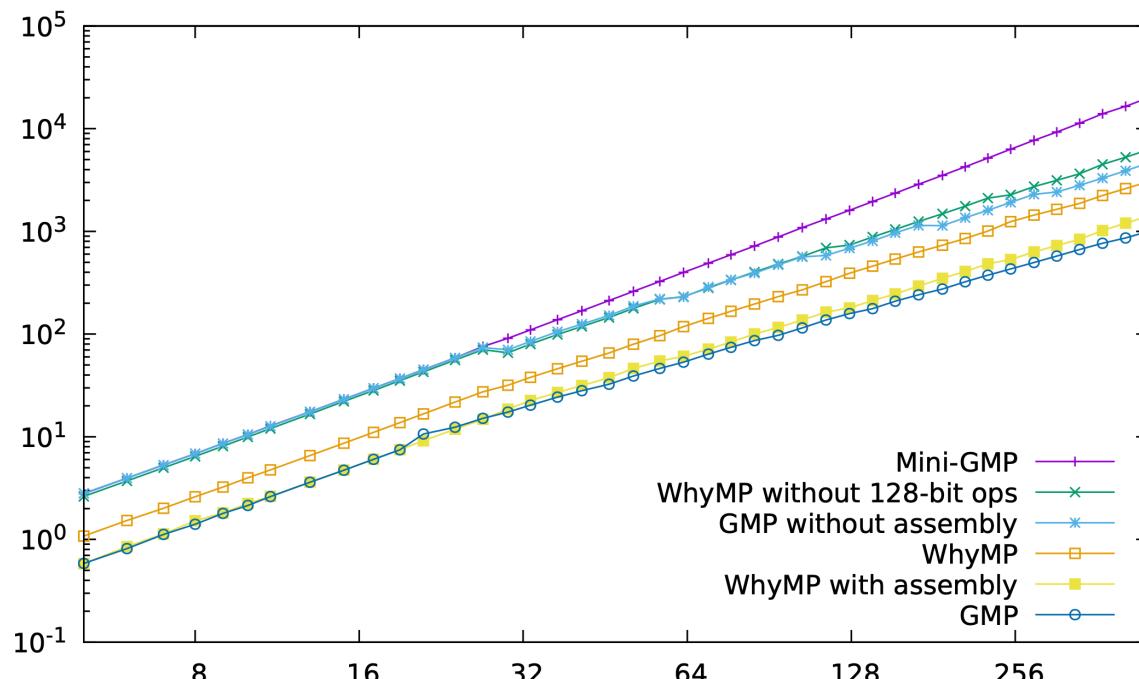
# A Why3 proof of GMP algorithms

Raphaël Rieu-Helft

TrustInSoft

Inria

Large-integer arithmetic algorithms are used in contexts where both their performance and their correctness are critical, such as cryptographic software. The fastest algorithms are complex enough that formally verifying them is desirable but challenging. We have formally verified a comprehensive arbitrary-precision integer arithmetic library that implements many state-of-the-art algorithms from the GMP library. The algorithms we have verified include addition, subtraction, Toom-Cook multiplication, division and square root. We use the Why3 platform to perform the proof semi-automatically. We obtain an efficient and formally verified C library of low-level functions on arbitrary-precision natural integers. This verification covers the functional correctness of the algorithms, as well as the memory safety and absence of arithmetic overflows of their C implementation. Using detailed pseudocode, we present the algorithms that we verified and outline their proofs.



## 1.1 Documents Index

1. [SPM](#) Documentation (this page)
  2. [ARG\\_TOOL](#) Toolkit Presentation
  3. [ARG\\_SPM](#) Formal Model Presentation
  4. [ARG\\_CDS](#) Correspondance with TOE Security Function Requirements (SFR)
  5. [ARG\\_FSP](#) Connections to TOE Functional Specifications (TSFI)
  6. [ARG\\_PROOF](#) Model Hypotheses Rationale

## 1.2 References Index

- JCRE JavaCard Runtime Environment
  - JCVM JavaCard Virtual Machine
  - SFR TOE Security Function Requirements
  - TSFI TOE Functional Specifications
  - SRS\_VM COSMO JavaCard Virtual Machine
  - SRS\_BIOS COSMO Basic Input/Output System BIOS
  - SPM\_HYP SPM Hypotheses

### 1.3 SPM Security Properties

- **spm** Abstract & Concrete Models Consistency
  - **jcre** JCRE Abstract Model
  - **security** Security Properties
  - **firewall** JCRE Firewall Specifications
  - **monitor** Security Monitor

## 1.4 COSMO VM Main Modules

- card Card External Interface
  - vm Internal VM State
  - apdu APDU Interpreter
  - bytecode Bytecode Interpreter
  - vmarea Memory Area Manager
  - vmstack Stack Frame Manager
  - vmcard Card Management Entry Points
  - bc Access Firewall Active Context Management

## 1.5 Taint Analysis

- `asset` Abstract Assets
  - `taint` Generic Taint Analysis



# Certificate

#### TRUST AND VERIFY

Standard	ISO/IEC 15408-1 :2009, -2 :2008, -3 :2008, Common Criteria for Information Technology Security Evaluation (CC) v3.1 rev 5 and ISO/IEC 18045 :2008, Common Criteria Evaluation Methodology for Information Security Evaluation (CEM) v3.1 rev 5
Certificate number	<b>NSCIB-CC-2300050-01</b>
	TrustCB B.V. certifies:
Certificate holder and developer	<b>IDEEDIA</b> <b>2 place Samuel de Champlain 92400, Courbevoie. France</b>
Product and assurance level	<b><u>ID-One Cosmo X</u></b> Assurance Package: <ul style="list-style-type: none"><li>▪ EAL6 augmented with ALC_FLR.1</li></ul> Protection Profile Conformance: <ul style="list-style-type: none"><li>▪ Java Card System – Open Configuration Protection Profile, Version 3.0.5 December 2017, BSI-CC-PP-0099-2017</li></ul>

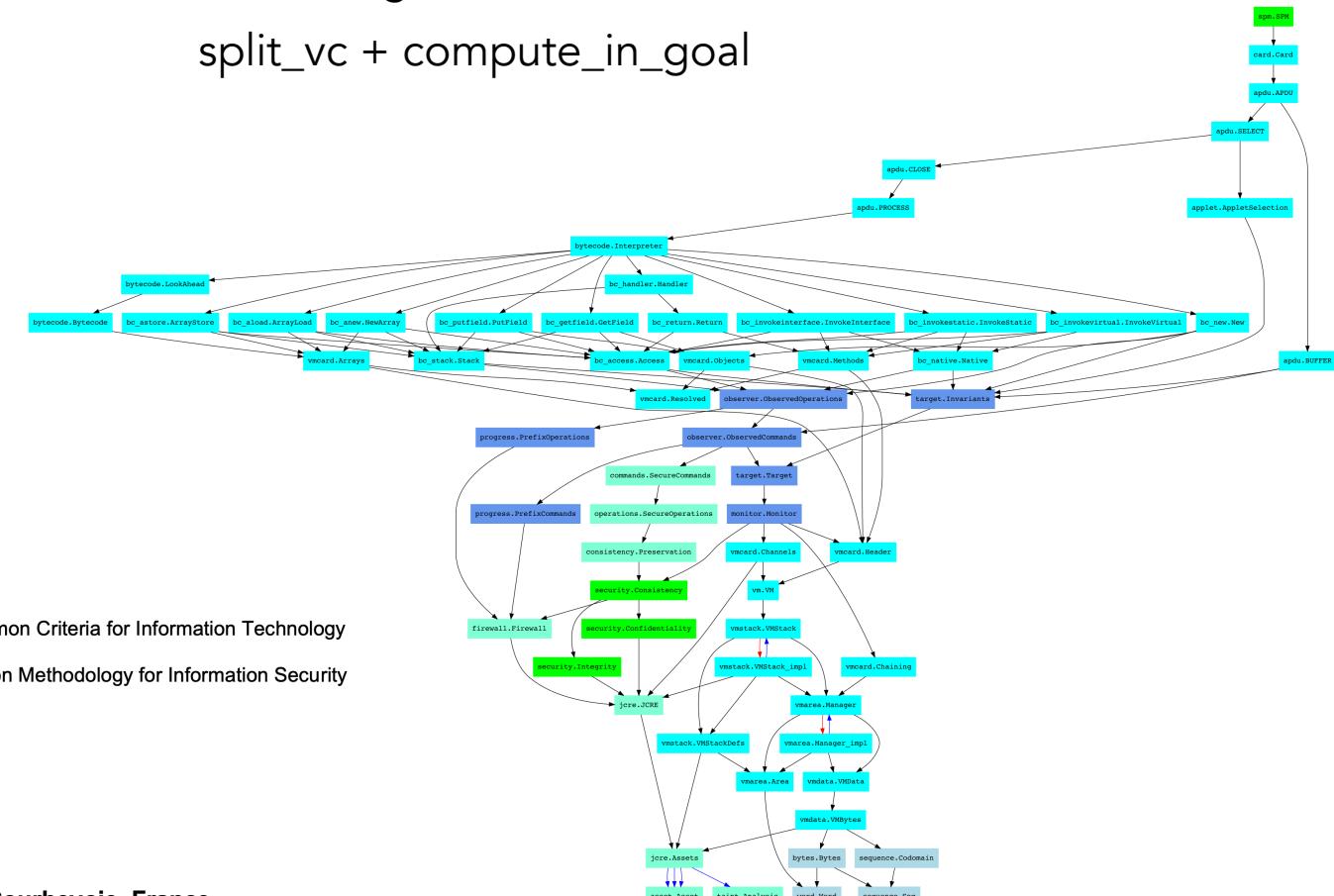
## Sources 10 kloc (mlw)

Doc 5 kloc (mc)

~2500 Preuve

## Alt-Ergo + z3 + cvc4

split\_vc + compute\_in\_goal



⟨⟩ IDEMIA



# Passage à l'échelle ?

---

## Questions de génie logiciel :

- ➔ Modularité
- ➔ Preuves automatiques vs interactives
- ➔ Puissance de calcul (parallélisation)
- ➔ Maintenance (dépendances)
- ➔ Collaboration (versions, co-développement)
- ➔ Partage (bibliothèque)

## Questions de confiance :

- ➔ Reproductibilité (configuration, temps de preuve)
- ➔ Base de confiance (hypothèses, axiomes)
- ➔ Documentation

# why3find

---

faciliter :  
le développement,  
la vérification et l'audit,  
la collaboration et le partage,  
pour et avec Why3 !



# why3find

---



\$ opam install why3find



## 📄 README.md

Tests

passed

Coverage

53.21%

## Why3 Library Manager

The `why3find` utility is dedicated to the management of Why3 packages. In short, from `why3find` point of view, a why3 package is a collection of why3 source files and associated documentation and OCaml extracted code that are installed at predefined site(s). It is designed to be fully compatible with Dune and OPAM.

- [Why3 Packages](#)
- [Package Development](#)
- [Package Configuration](#)
- [Package Proving](#)
- [Package Documentation](#)
- [Package Soundness](#)
- [OCaml Code Extraction](#)

# why3find

---

```
$ why3find --help
why3find [-h|--help]
why3find [-v|--version]
why3find where
why3find shared
why3find init
why3find list
why3find query [PKG...]
why3find config [OPTIONS] PROVERS
why3find prove [OPTIONS] PATH...
why3find doc [OPTIONS] PATH...
why3find extract [OPTIONS] MODULE...
why3find server OPTIONS
why3find worker OPTIONS
why3find install PKG PATH...
why3find uninstall [PKG...]
why3find compile [-p PKG] FILE
why3find ide [-p PKG] FILE
why3find replay [-p PKG] FILE
why3find CMD [ARGS...]
```

# JFLA 2024

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- A. Preuves
- B. Hypothèses
- C. Documentation

# Preuves

---

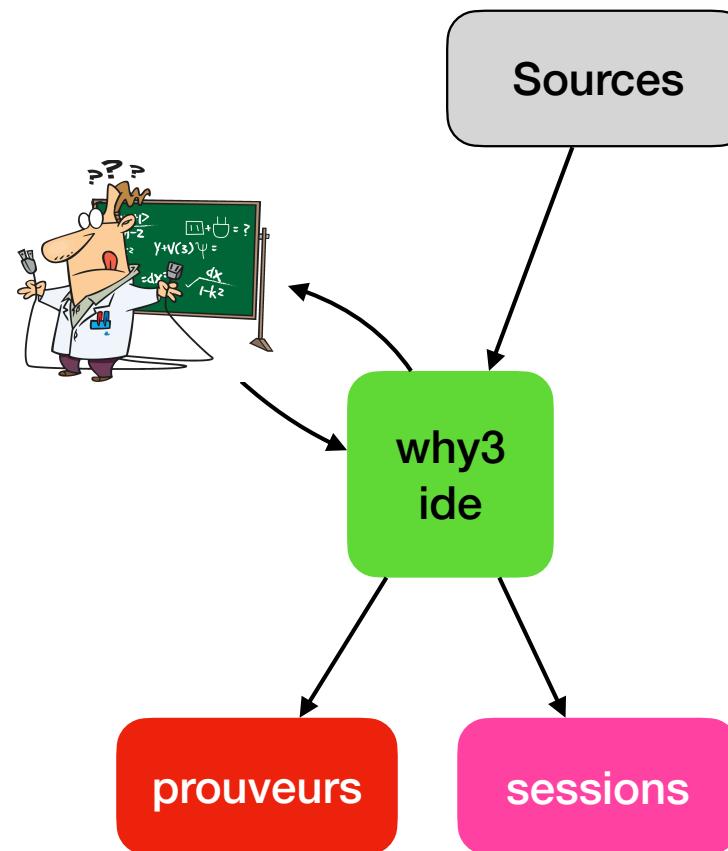
Automatisation

Maintenance

Reproductibilité

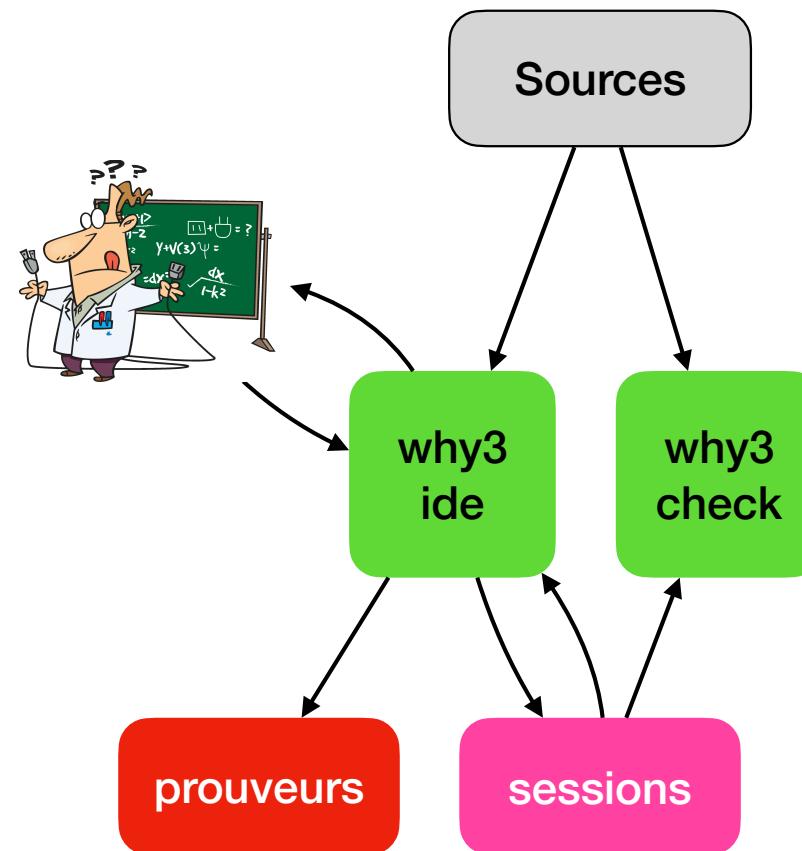
# Why3 workflow

---



# Why3 workflow

---



Why3 Interactive Proof Session

File Edit Tools View Help

Status Theories/Goals

Task security.mlw

```

222  a central role in the preservation of owner's context. This property is
223  then necessary to prove the preservation of confidentiality and integrity,
224  typically in presence of context switches. *)
225
226 let rec lemma package_invariant (s: system) (op: operations)
227   ensures { s.capfile = (execute s op).capfile }
228   ensures { s.installed = (execute s op).installed }
229 (*proof*)
230 variant { op }
231 = match op with
232 | Nop -> ()
233 | Invoke (Static as m) xs p _ ->
234   package_invariant (switch_context s m xs) p
235 | Invoke (Entry_point _ as m) xs p _ ->
236   package_invariant (switch_context s m xs) p
237 | Invoke (Method _ as m) xs p _ ->
238   package_invariant (switch_context s m xs) p
239 | Invoke (Shareable _ as m) xs p _ ->
240   package_invariant (switch_context s m xs) p
241 | Sequence p q ->
242   package_invariant s p ;
243   package_invariant (execute s p) q ;
244 | Stack _ _ -> ()
245 | Read _ _ -> ()
246 | Write obj _ ->
247   if leaked s obj then () else
248   if s.active = JCRE_context then () else
249   ()
250 | Create _ _ _ _ -> ()
251 | Delete _ _ _ -> ()
252 end
253 (*qed*)
254

```

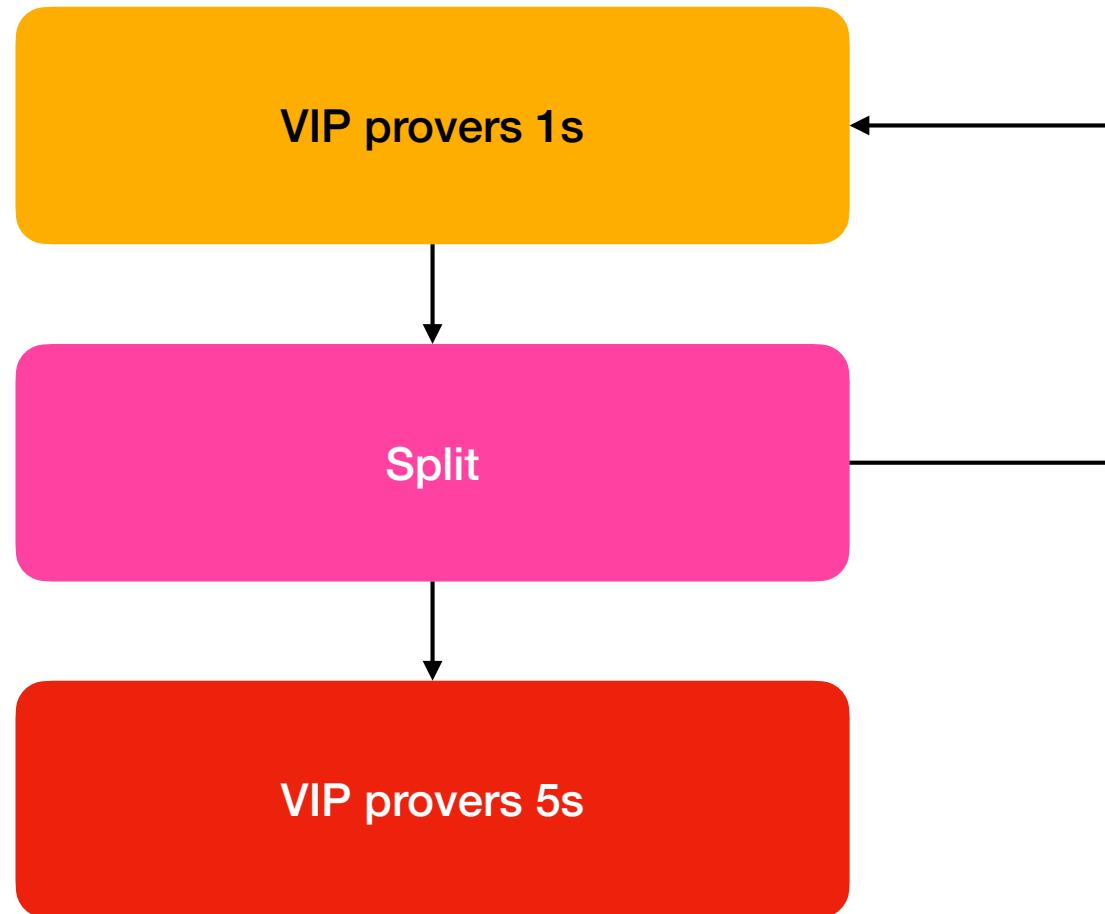
0/0/0 type commands here

Messages Log Edited proof Prover output Counterexample

- integrity\_transfervc [VC for integrity\_transfer]
- package\_invariantvc [VC for package\_invariant]
  - Alt-Ergo 2.4.2
  - Z3 4.8.15
  - CVC4 1.8
- split\_vc
  - 0 [variant decrease]
  - 1 [variant decrease]
  - 2 [variant decrease]
  - 3 [variant decrease]
  - 4 [variant decrease]
  - 5 [variant decrease]
  - 6 [postcondition]
    - Alt-Ergo 2.4.2
    - Z3 4.8.15
    - CVC4 1.8
  - split\_vc
    - 0 [postcondition]
      - Alt-Ergo 2.4.2
    - 1 [postcondition]
    - 2 [postcondition]
    - 3 [postcondition]
    - 4 [postcondition]
  - 5 [postcondition]
    - 6 [postcondition]
    - 7 [postcondition]
    - 8 [postcondition]
    - 9 [postcondition]
    - 10 [postcondition]
  - 7 [postcondition]
- consistent\_owner\_transfervc [VC for consistent\_owner\_transfer]
- consistent\_domain\_transfervc [VC for consistent\_domain\_transfer]
- consistent\_object\_transfervc [VC for consistent\_object\_transfer]

# why3 ide — auto-level 2 & 3

---



# Les preuves à l'épreuve du réel...

---

## Automatisation

- ➔ Prouveurs (interactifs, automatiques)
- ➔ Transformations (stratégies, transformations)

## Maintenance

- ➔ Recherche incrémentale
- ➔ Cache de prouveurs
- ➔ Dépendances

## Reproductibilité

- ➔ Temps limite de preuve (changement de machine)
- ➔ Sessions why3 (machine, volatile, merge)
- ➔ Rejeu, audit ?



No More  
Interactive Provers !

Go to IDE  
for DEBUG only !

Use Split &  
Lemma Functions !

# Des routines avec des contrats...

---

```
let wmpn_copyi (r x: ptr uint64) (n: int32) : unit
  requires { valid x n ∧ valid r n }
  ensures { forall i. 0 ≤ i < n → r[i] = x[i] }
  ensures { forall i. i < 0 ∨ n ≤ i → r[i] = old r[i] }
= let ref i = 0 in
  while (Int32.(<) i n) do
    variant { n - i }
    invariant { forall j. 0 ≤ j < i → r[j] = x[j] }
    invariant { forall j. j < 0 ∨ i ≤ j → r[j] = old r[j] }
    r[i] ← x[i];
    i ← i+1;
  done
```

# Logique de Hoare

---

```
let foo  x y : τ
    requires  H(x, y)
    returns  r ↠ P(x, y, r)
    = (* code *)
```

# Logique de Hoare

---

```
let foo     $x\ y : \tau$ 
    requires    $H(x, y)$ 
    returns     $r \mapsto P(x, y, r)$ 
    = (* code *)
```

theorem **foo-wp** :

$$\forall x, y . H(x, y) \rightarrow \text{let } r = \text{foo } x\ y \text{ in } P(x, y, r)$$

# Logique de Hoare & Isomorphisme de Curry-Howard

---

```
let foo     $x\ y : \tau$ 
    requires    $H(x, y)$ 
    returns     $r \mapsto P(x, y, r)$ 
    = (* code *)
```

theorem **foo-lemma** :

$$\forall x, y . H(x, y) \rightarrow \exists r . P(x, y, r)$$

# Lemma Functions

---

```
let lemma prod_compat_r (a b c:int)
  requires { 0 ≤ a ≤ b }
  requires { 0 ≤ c }
  ensures { c * a ≤ c * b }
= ()
```

$\forall a, b, c \in \mathbb{Z}, 0 \leq a \leq b \wedge 0 \leq c \implies ca \leq cb$

```
let lemma prod_compat_lr (a b c d:int)
  requires { 0 ≤ a ≤ b }
  requires { 0 ≤ c ≤ d }
  ensures { a * c ≤ b * d }
= prod_compat_r c d a; (* ac ≤ ad *)
  prod_compat_r a b d   (* da ≤ db *)
```

$\forall a, b, c, d \in \mathbb{Z}, 0 \leq a \leq b \wedge 0 \leq c \leq d \implies ac \leq bd$

# Lemma Functions

---

```
let lemma fact_div (x y z:int)
  requires { y > 0 }
  ensures { div (x + y * z) y = (div x y) + z }
=
  assert { div (x + y * z) y = (div x y) + z
    by x + y * z = y * (div (x + y * z) y) + mod (x + y * z) y
    so mod (x + y * z) y = mod (y * z + x) y = mod x y
    so x + y * z = y * (div (x + y * z) y) + mod x y
    so x = y * div x y + mod x y
    so x + y * z = y * div x y + mod x y + y * z
    so y * (div (x + y * z) y) + mod x y
      = y * div x y + mod x y + y * z
    so y * (div (x + y * z) y)
      = y * div x y + y * z
      = y * ((div x y) + z)
    so div (x + y * z) y = div x y + z }
```

# Lemma Functions (inductive case)

---

$$\forall n \in \mathbb{Z}, 0 \leq n \implies n \leq 2^n$$

# Lemma Functions & preuves par induction

---

$$\forall n \in \mathbb{Z}, 0 \leq n \implies n \leq 2^n$$

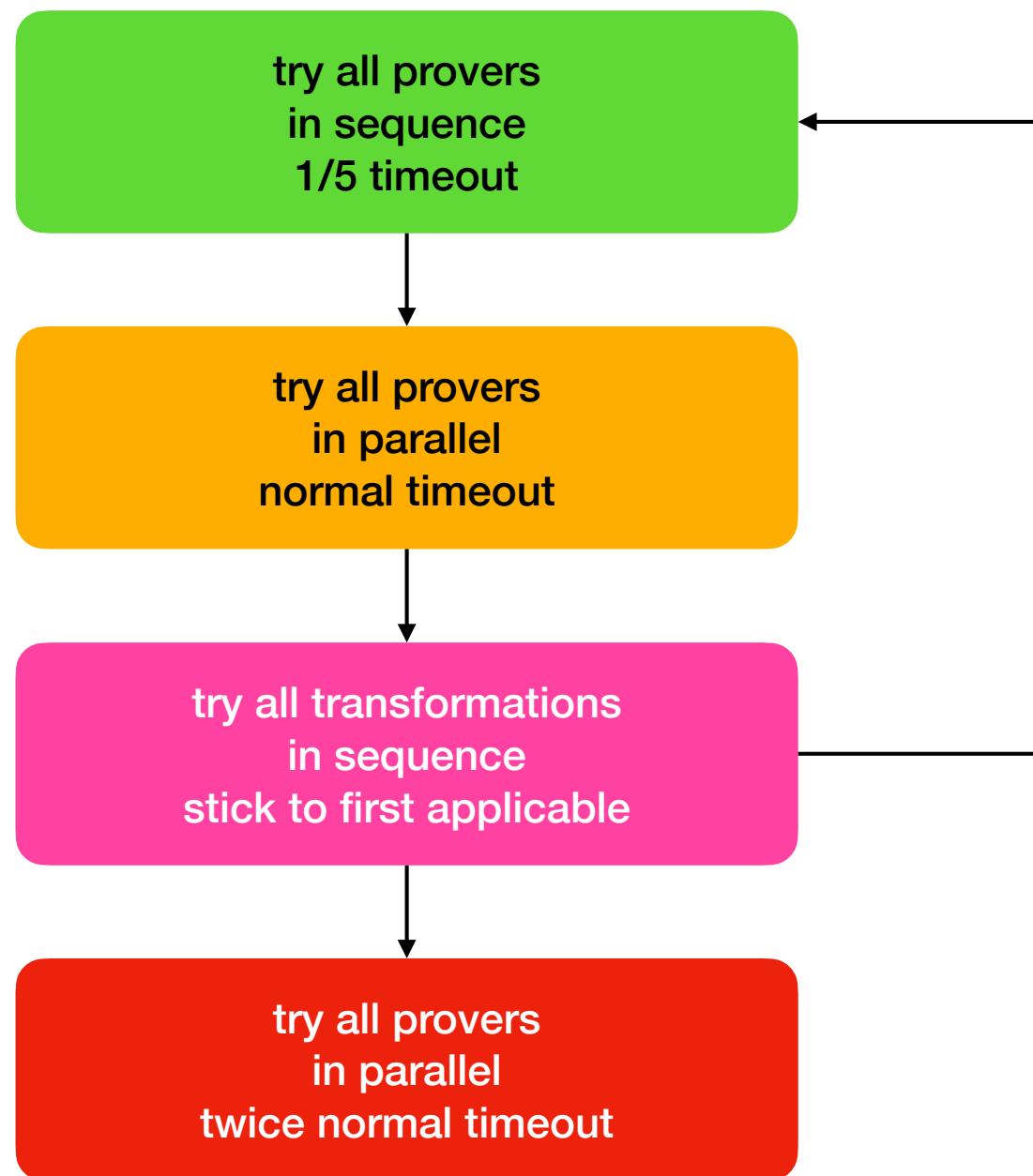
```
let rec lemma pow2_gt (n:int)
  requires { 0 ≤ n }
  ensures { n ≤ power 2 n }
  variant { n }
= if n > 0 then pow2_gt (n-1)
```

# why3find proof strategy

---

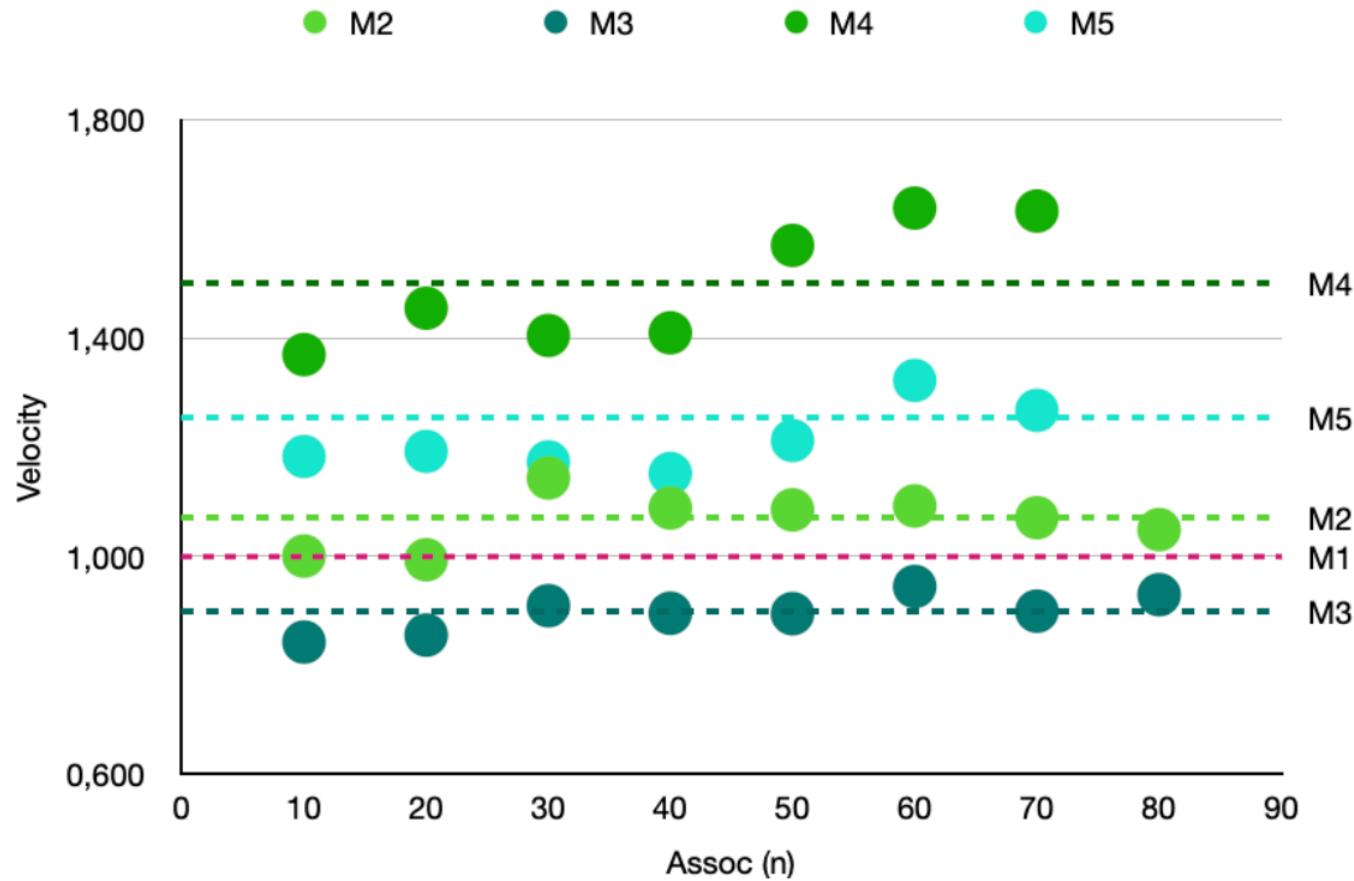


why3find config  
why3find prove [options]



# Calibrage des prouveurs

---



**Figure 1.** Experimenting the Velocity Law.

# Témoins de preuve

$$c ::= \perp \mid \pi : t \mid \tau(c_1, \dots, c_n)$$

---

```
$ cat sequence/proof.json
{
  "profile": [
    { "prover": "Alt-Ergo,2.4.2", "size": 17, "time": 0.8175 },
    { "prover": "CVC4,1.8", "size": 40, "time": 0.36 },
    { "prover": "Z3,4.8.15", "size": 34, "time": 0.87 }
  ],
  "proofs": {
    "Seq": {
      "mixfix []": { "prover": "alt-ergo", "time": 0.007 },
      "head": { "prover": "alt-ergo", "time": 0.004 },
      "tail": { "prover": "alt-ergo", "time": 0.004 },
      "reflexivity": { "prover": "alt-ergo", "time": 0.003 },
      "extensivity": { "prover": "alt-ergo", "time": 0.041 },
      "equal": { "prover": "alt-ergo", "time": 0.033 },
      "hd": { "prover": "alt-ergo", "time": 0.004 },
      "tl": { "prover": "alt-ergo", "time": 0.003 },
      "create": { "prover": "alt-ergo", "time": 0.006 },
      "reset": { "prover": "alt-ergo", "time": 0.003 },
      "init": { "prover": "alt-ergo", "time": 0.009000000000000001 },
      "map": { "prover": "alt-ergo", "time": 0.01 },
      "infix ++": { "prover": "alt-ergo", "time": 0.02600000000000002 },
      "mixfix [..)": { "prover": "alt-ergo", "time": 0.038 },
      "mixfix [.._]": { "prover": "alt-ergo", "time": 0.006 },
      "mixfix [_..)": { "prover": "alt-ergo", "time": 0.006 },
      "split": {
        "tactic": "split_vc",
        "children": [
          { "prover": "alt-ergo", "time": 0.02 },
          { "prover": "alt-ergo", "time": 0.004 }
        ]
      },
      "fullsplit": {
        "tactic": "split_vc",
        "children": [
          { "prover": "alt-ergo", "time": 0.032 },
          { "prover": "alt-ergo", "time": 0.01 }
        ]
      },
      "infix +.": { "prover": "alt-ergo", "time": 0.007 },
      "infix .+": { "prover": "alt-ergo", "time": 0.008 },
      "mixfix [<-]": { "prover": "alt-ergo", "time": 0.02 },
      "memcpy": { "prover": "alt-ergo", "time": 0.049 }
    },
    "Codomain": { "codomain": { "prover": "z3", "time": 0.18 } }
  }
}
```

# Tout en ligne de commande !

---

```
$ why3find prove -i      # debug within IDE  
$ why3find prove -f      # force rebuild proof  
$ why3find prove -m      # minimize proof tree  
$ why3find prove -r      # replay from certificate
```

# Hypothèses

---

Traçabilité

Incohérences

# Requirements on the Use of Coq in the Context of Common Criteria Evaluations

French National Cybersecurity Agency (ANSSI)  
INRIA

V1.0 23/09/2020

## 4.1 Axioms and Hypotheses

Coq allows for introducing opaque, well-typed constants which lack a body, that is a term of the expected type. One notable way to achieve this is the **Parameter** vernacular command (or its synonyms, *e.g.*, **Variable**, **Hypothesis**, etc.).

**Evaluators Rule 4.1.** Starting from Coq 8.5, the **Print Assumptions** command shall be used in order to determine which constants lacking a definition body have been used to prove key theorems.

# C'est de la triche !

---

```
val f () : int
  ensures { result > 0 }
  ensures { result < 0 }
```



# Modules & clones

---

**module A**

$x_1 : t_1 \dots x_n : t_n$

**end**

**module  $M$**

$\dots$

**clone  $A$  with  $x_1 = a_1, \dots, x_n = a_n$**

$\dots$

**end**

# Envoyez les clones !

---

module  $M$

...

clone  $A$  with  $x_1 = a_1, \dots, x_n = a_n$

...

end



# C'est (encore) de la triche !

---

```
let f () : int
    ensures { result > 0 }
    ensures { result < 0 }
= assume { false } ; any int
```



# Consolidation des Hypothèses

---

Tout module avec des hypothèses  
doit avoir une instance (transitivement) close

La construction « assume » est interdite

Traçabilité dans la documentation

# Documentation

---

Spécifications vs. Code vs. Preuves

# Verified Correctness, Accuracy, and Convergence of a Stationary Iterative Linear Solver: Jacobi Method

Mohit Tekriwal<sup>1</sup>, Andrew W. Appel<sup>2</sup>, Ariel E. Kellison<sup>3</sup>, David Bindel<sup>3</sup>, and  
Jean-Baptiste Jeannin<sup>1</sup>

<sup>1</sup> University of Michigan, USA `{tmohit, jeannin}@umich.edu`

<sup>2</sup> Princeton University, USA `appel@princeton.edu`

<sup>3</sup> Cornell University, USA `{ak2485, bindel}@cornell.edu`

**Abstract.** Solving a sparse linear system of the form  $Ax = b$  is a common engineering task, e.g., as a step in approximating solutions of differential equations. Inverting a large matrix  $A$  is often too expensive, and instead engineers rely on iterative methods, which progressively approximate the solution  $x$  of the linear system in several iterations, where each iteration is a much less expensive (sparse) matrix-vector multiplication.

We present a formal proof in the Coq proof assistant of the correctness, accuracy and convergence of one prominent iterative method, the Jacobi iteration. The accuracy and convergence properties of Jacobi iteration are

## Documentation

- ➔ Un peu de style (markdown)
- ➔ Structure, pagination (literate)
- ➔ Parties cachées (preuves, remarques, etc.)
- ➔ Pages de documentation (hors sources)
- ➔ Liens inter-paquets

## Consolidation

- ➔ Témoins de preuve
- ➔ Complétude des preuves
- ➔ Traçabilité des hypothèses
- ➔ Signature des clones
- ➔ Clones sans instance close

# Conclusion

---

## Faire des paquets de preuves ?

- ➔ Développement
- ➔ Maintenance
- ➔ Reproductibilité
- ➔ Documentation
- ➔ Distribution

# Happy Proving !

---



\$ opam install why3find